

Kalman Filter Implementation

AE 5621 – GNC

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Introduction

The drone industry has experienced exponential growth in the past two decades, primarily driven by advancements in aerospace technology. The Federal Aviation Administration (FAA) has eased restrictions on controlled airspaces for drones, potentially paving the path for revolutionizing industries that utilize drones. Agriculture, logistics, and surveillance drone usage have skyrocketed since this gradual change. Among these developments, small quadrotors have emerged as market leaders due to their affordability and versatility, despite challenges in flight performance.

At the core of a successfully performing drone lies the need for accurate motion and acceleration measurement, which heavily relies on an efficient and cost-effective Inertial Measurement Unit (IMU). IMUs have decreased in cost significantly while maintaining high-performance stability integration. Paired with a microcontroller, such as an Arduino, these IMUs hold significant promise for improving the flight stability and maneuverability of drones.

The focus of this project is to implement a Kalman Filter to enhance the performance of an IMU by filtering noise and providing accurate estimates of pitch and roll angles. The Kalman Filter is widely recognized in the aerospace industry as a leader in real-time system identification and addressing inaccuracies of cheaper IMUs. By using MATLAB to integrate this filter into a BNO055 9-axis IMU, this project aims to demonstrate improved motion tracking in various pitch and roll maneuvers.

Hardware Description

The hardware provided for this project consists of the following:

1. Arduino UNO Rev3
2. BNO-055 9-axis IMU
3. Mini breadboard
4. 4 jumper wires (for wiring setup)

The Arduino UNO is a popular microcontroller board based on the ATmega328P microcontroller. It is widely used for electronics projects and prototyping due to its simplicity and versatility. For this project, it will be useful for interfacing the IMU with computer software. It is powered through a USB connection to a computer. The USB connection is also used for programming and serial communications. There are several standard 0.1-inch pitch headers for easy connection. The board is configured for male pins but can use stacking headers for shields. There is also an ICSP header that allows for direct programming of the board using an In-Circuit Serial Programmer. Several LED indicators on the board allow the user to tell whether it is powered on and functioning properly.

The BNO-055 9-axis IMU is integrated into the Arduino board to allow for sensor fusion. It combines a 3-axis gyroscope, 3-axis accelerometer, and 3-axis magnetometer, along with an ARM Cortex-M0 processor to perform real-time sensor fusion and communicate orientation data. The device combines raw motion sensing with onboard sensor fusion algorithms to deliver a mostly ready-to-use output. However, as with many cheap IMUs, sensor noise is visible when monitoring the system. Thus, it is important that noise filtering algorithms are implemented on the software side to deliver drift-compensated outputs to the user.

The main purpose of the breadboard is simply to connect the IMU and the Arduino boards. The mini breadboard completes the setup and allows the testbed to function properly. The jumper wires are used to connect the breadboard to the Arduino board. The IMU is soldered to the breadboard using pins.

Figure 1 shows the completed setup that includes the IMU, Arduino, and breadboard.

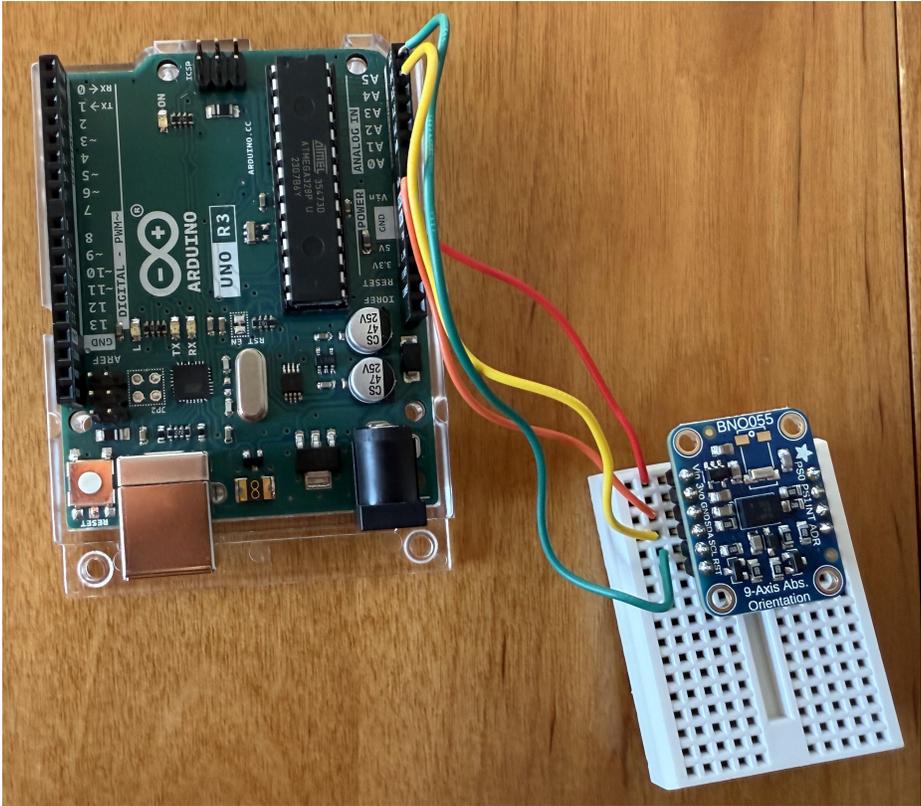


Figure 1: Wired Arduino board and IMU for full hardware setup

Additionally, Figure 2 displays the required wiring diagram that was used to complete the setup above.

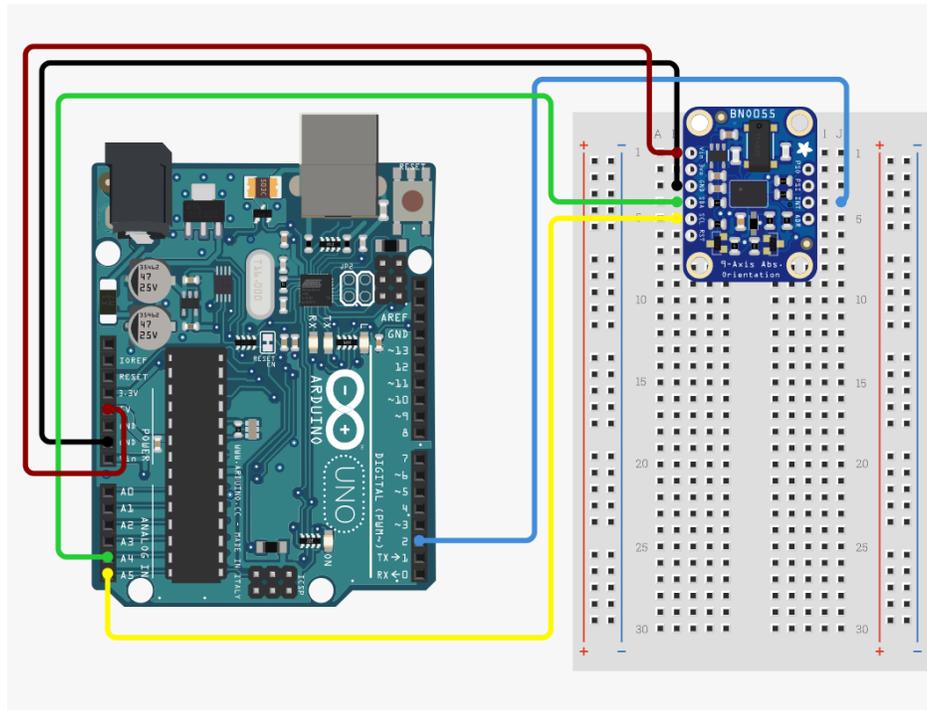


Figure 2: Full wiring diagram for hardware setup

The ports used on the Arduino board are A5, A4, GND, and 5V. These were connected to SCL, SDA, GND, and Vin on the IMU board respectively. The 5V pin provides the power supply to the voltage input in the IMU and the ground pins on each board are simply ground wires. I2C communication is done through the A4 pin on the Arduino which is connected to the SDA or Serial Data pin on the sensor. The A5 pin from the Arduino connects to the Serial Clock (SCL) pin on the sensor to allow for smooth data exchange. This setup is quite simple, yet effective when using the Arduino and IMU provided.

Theory and Implementation

A Kalman Filter is an effective state estimator for a process by predicting the future state based on the measurement of the prior state while accounting for error in measurement and sensing. The filter that is implemented in this work is an Extended Kalman Filter (EKF) which offers state estimation for non-linear systems. Reliance on Euler angle computations from gyroscope and accelerometer readings can lead to computational errors and undetermined states. The EKF will be computed using quaternions which avoid any singularities in the computation.

The procedure of the filter is a recursive loop that consists of projecting the future state, projecting the future error covariance, updating the estimate, and finally updating the error covariance. Future state prediction is given by

$$\hat{x}_k^- = f(\hat{x}_{k-1}, u_{k-1}, w_{k-1}) \quad (1)$$

where \hat{x}_k^- is the projected state, \hat{x}_{k-1} is the previous state measurement, u_{k-1} is the previous measured input, and w_{k-1} is random measurement noise from the previous step. For our purposes, w_{k-1} cannot be known, thus our new state prediction is

$$\hat{x}_k^- = f(\hat{x}_{k-1}, u_{k-1}, 0) \quad (2)$$

Reading of the gyroscope rates allows input to the system for Euler angles ϕ, θ, ψ . Input from the gyros is given as:

$$\dot{\phi} = p + q \sin \psi \tan \theta + r \cos \psi \tan \theta \quad (3)$$

$$\dot{\theta} = q \cos \psi - r \sin \psi \quad (4)$$

$$\dot{\psi} = q \sin \psi \sec \theta + r \cos \psi \sec \theta \quad (5)$$

P, q, r can be expressed as $\omega_1, \omega_2, \omega_3$ respectively. Equations (3)–(5), when expressed in quaternion matrix form, become the following:

$$\begin{bmatrix} \dot{q}_1 \\ \dot{q}_2 \\ \dot{q}_3 \\ \dot{q}_4 \end{bmatrix} = \frac{1}{2} \begin{bmatrix} 0 & \omega_3 & -\omega_2 & \omega_1 \\ -\omega_3 & 0 & \omega_1 & \omega_2 \\ \omega_2 & -\omega_1 & 0 & \omega_3 \\ -\omega_1 & -\omega_2 & -\omega_3 & 0 \end{bmatrix} \begin{bmatrix} q_1 \\ q_2 \\ q_3 \\ q_4 \end{bmatrix} \quad (6)$$

Discretizing by derivative approximation, combining equations (2) and (6) yields the state predictor

$$\hat{x}_k^- = \begin{bmatrix} q_{1k} \\ q_{2k} \\ q_{3k} \\ q_{4k} \end{bmatrix} = \frac{h}{2} \begin{bmatrix} 2/h & \omega_3 & -\omega_2 & \omega_1 \\ -\omega_3 & 2/h & \omega_1 & \omega_2 \\ \omega_2 & -\omega_1 & 2/h & \omega_3 \\ -\omega_1 & -\omega_2 & -\omega_3 & 2/h \end{bmatrix} \begin{bmatrix} q_{1k-1} \\ q_{2k-1} \\ q_{3k-1} \\ q_{4k-1} \end{bmatrix} \quad (7)$$

Covariance projection is given by

$$P_k^- = A_k P_{k-1} A_k^T + W_k Q_{k-1} W_k^T \quad (8)$$

where P_k^- is the projected covariance, A_k is a Jacobian matrix with respect to x , W_k is a Jacobian matrix with respect to w_k , and Q_{k-1} is process noise covariance. Because w_k is unknown, W_k will be assumed to be an identity matrix; Q_{k-1} will also be assumed to be constant and an identity matrix with an attached scalar ~ 0.0001 to account for the accuracy of the sensors. Equation (8) thus becomes

$$P_k^- = A_k P_{k-1} A_k^T + Q \quad (9)$$

The Jacobian A_k in quaternion format taken with respect to ω yields the same result as equation (6).

$$A_k = \frac{1}{2} \begin{bmatrix} 0 & \omega_3 & -\omega_2 & \omega_1 \\ -\omega_3 & 0 & \omega_1 & \omega_2 \\ \omega_2 & -\omega_1 & 0 & \omega_3 \\ -\omega_1 & -\omega_2 & -\omega_3 & 0 \end{bmatrix} \quad (10)$$

Kalman gain can be calculated from

$$K_k = P_k^- H_k^T (H_k P_k^- H_k^T + V_k R_k V_k^T)^{-1} \quad (11)$$

For our project, V_k and H_k are assumed to be identity matrices. The new form for Kalman gain is:

$$K_k = P_k^- (P_k^- + R_k)^{-1} \quad (12)$$

where R_k is the covariance of the measurement sensors. The covariance of the measurement sensors was calculated by allowing the IMU to lay flat on a table with no motion for approximately 3 minutes and using MATLAB to calculate the covariance of each sensor. Table 1 presents the results of these calculations.

Sensor	Covariance
Accel x	1.732×10^{-7}
Accel y	1.327×10^{-7}
Accel z	4.473×10^{-7}
Gyro x	4.125×10^{-7}
Gyro y	6.884×10^{-7}
Gyro z	4.011×10^{-7}

Table 1: Covariance calculations from sensors

Once the Kalman gain is computed, the update portion of the filter can start. The equation for the state update is given by

$$\hat{x}_k = \hat{x}_k^- + K_k (z_k - h(\hat{x}_k^-, 0)) \quad (13)$$

where z_k is a measurement provided by a sensor. The measurement will be provided by the accelerometers of the IMU, and Euler angles can be calculated as

$$\theta = \sin^{-1} \left(\frac{a_x}{g} \right) \quad (14)$$

$$\phi = \tan^{-1} \left(\frac{a_y}{a_z} \right) \quad (15)$$

$$\psi = 0 \quad (16)$$

Due to the sensitive nature of the onboard magnetometer, the measurement of ψ was consistently 0. When expressed in quaternion form, the measurement matrix becomes

$$z_k = \begin{bmatrix} q_{1k} \\ q_{2k} \\ q_{3k} \\ q_{4k} \end{bmatrix} = \begin{bmatrix} \sin \frac{\phi}{2} \cos \frac{\theta}{2} \\ \cos \frac{\phi}{2} \sin \frac{\theta}{2} \\ -\sin \frac{\phi}{2} \sin \frac{\theta}{2} \\ \cos \frac{\phi}{2} \cos \frac{\theta}{2} \end{bmatrix} \quad (17)$$

Update to error covariance is then given by:

$$P_k^- = (I - K_k) P_k^- \quad (18)$$

Once the state update is performed, a direction cosine matrix (DCM) can be constructed from new quaternions and the new best estimate for Euler angles:

$$\phi = \tan^{-1} \left(\frac{2(q_1q_2 + q_3q_4)}{q_1^2 - q_2^2 - q_3^2 + q_4^2} \right) \quad (19)$$

$$\theta = \sin^{-1} \left(\frac{-2(q_1q_3 + q_2q_4)}{\sqrt{(q_1^2 - q_2^2 - q_3^2 + q_4^2)^2 + (2(q_1q_2 + q_3q_4))^2}} \right) \quad (20)$$

$$\psi = \tan^{-1} \left(\frac{2(q_2q_3 + q_1q_4)}{q_3^2 - q_1^2 - q_2^2 + q_4^2} \right) \quad (21)$$

Experimental Results

The IMU was rotated from -30° to 30° for 10 seconds in only roll, only pitch, and combined roll and pitch maneuvers. Figures 3–5 present the results of the testing.

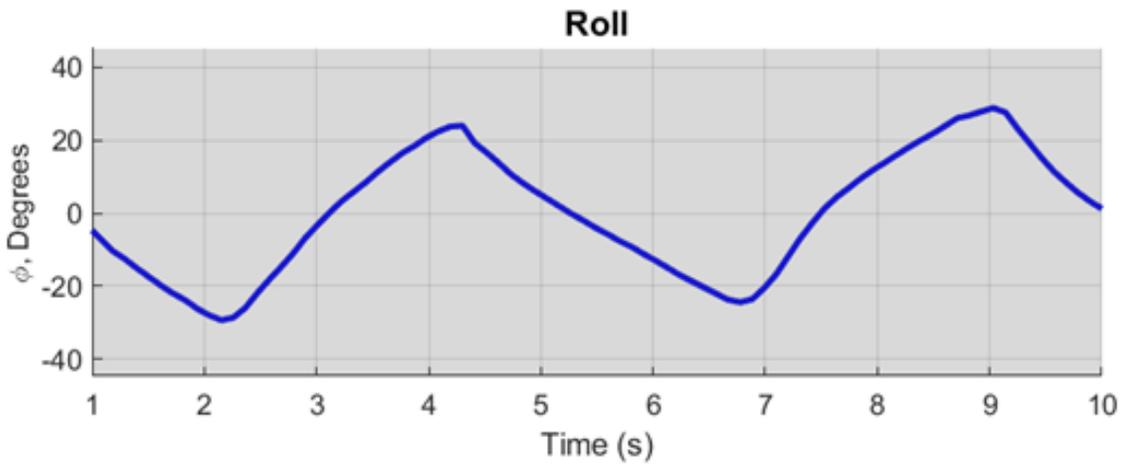


Figure 3: Roll from -30 degrees to 30 degrees, 10 seconds

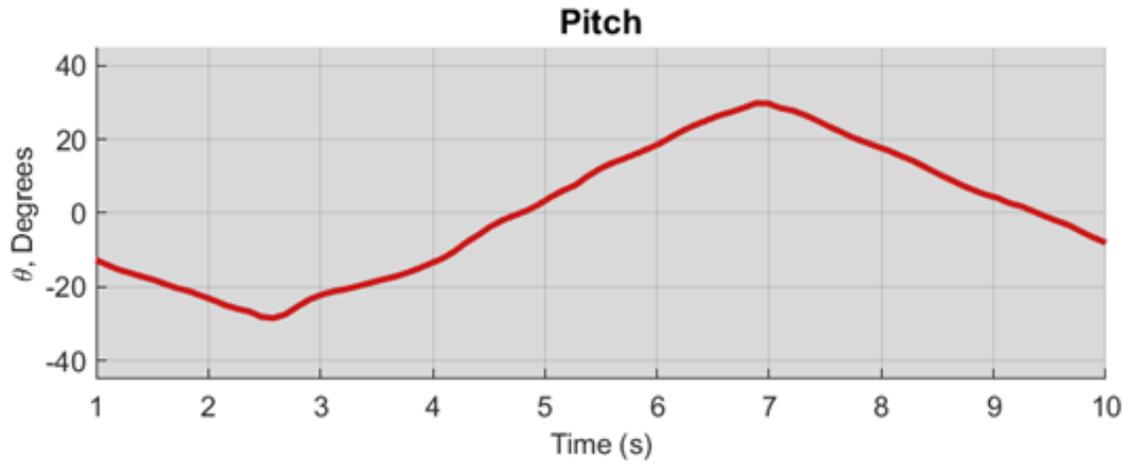


Figure 4: Pitch from -30 degrees to 30 degrees, 10 seconds

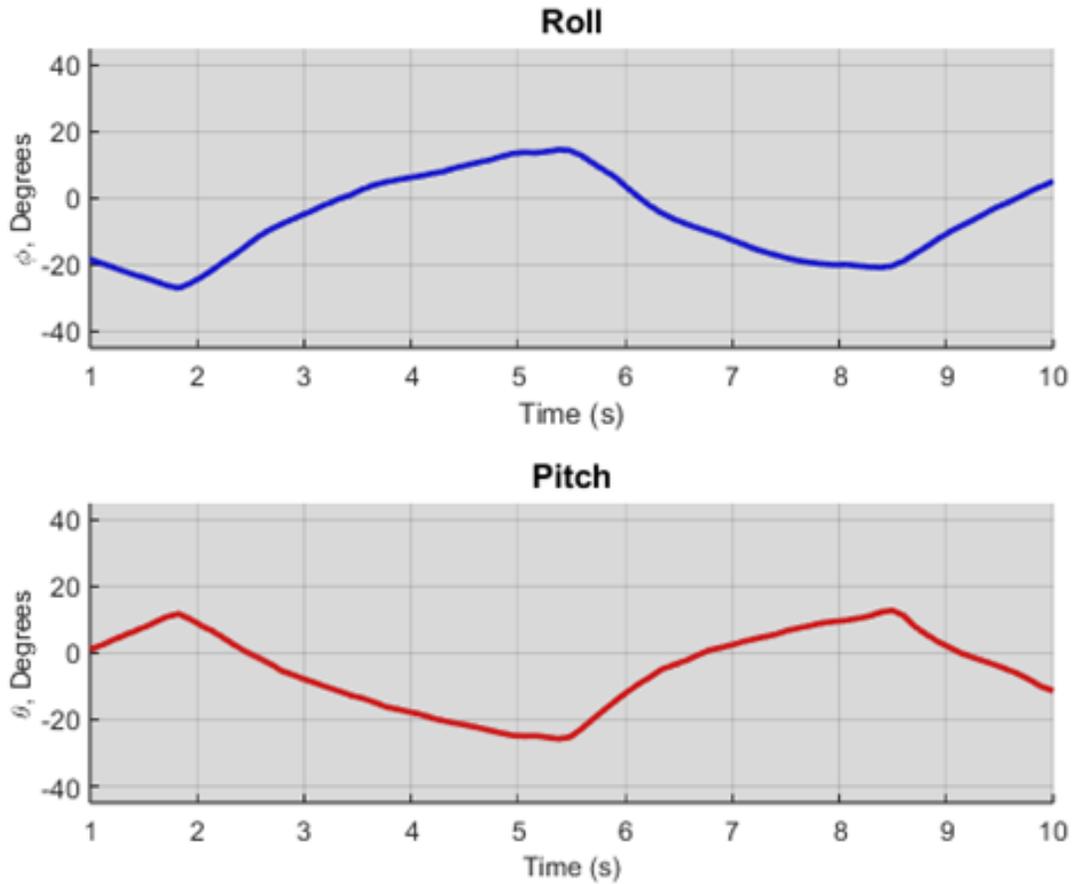


Figure 5: Pitch and Roll from -30 degrees to 30 degrees, 10 seconds

Clearly, the filter performed excellent state estimation and was quick to respond to gradual changes in angle and low frequencies. From Figure 5 with combined maneuvering, the

filter performed well, and the results are similar to both Figures 3 and 4. Next, the same tests were performed over a test period of 2 seconds. Figures 6–8 present the results.

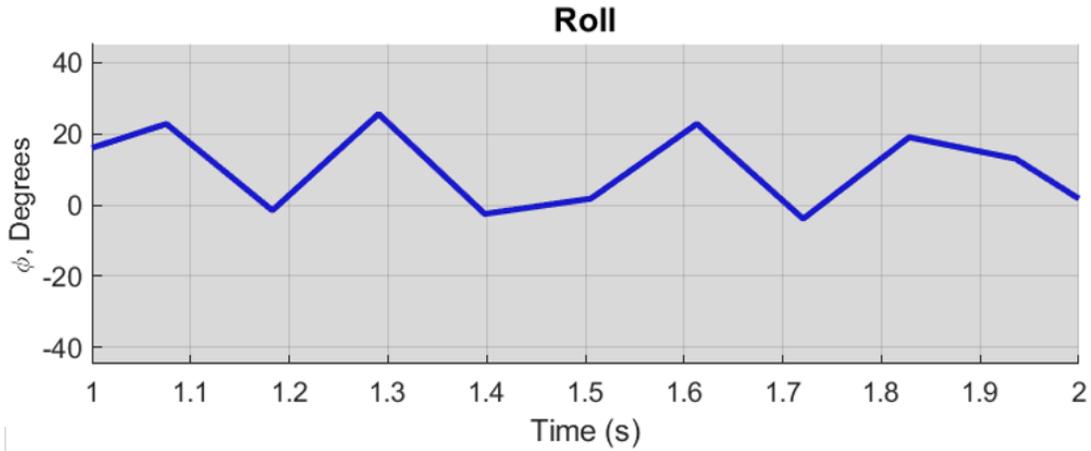


Figure 6: Roll from -30 degrees to 30 degrees, 2 seconds

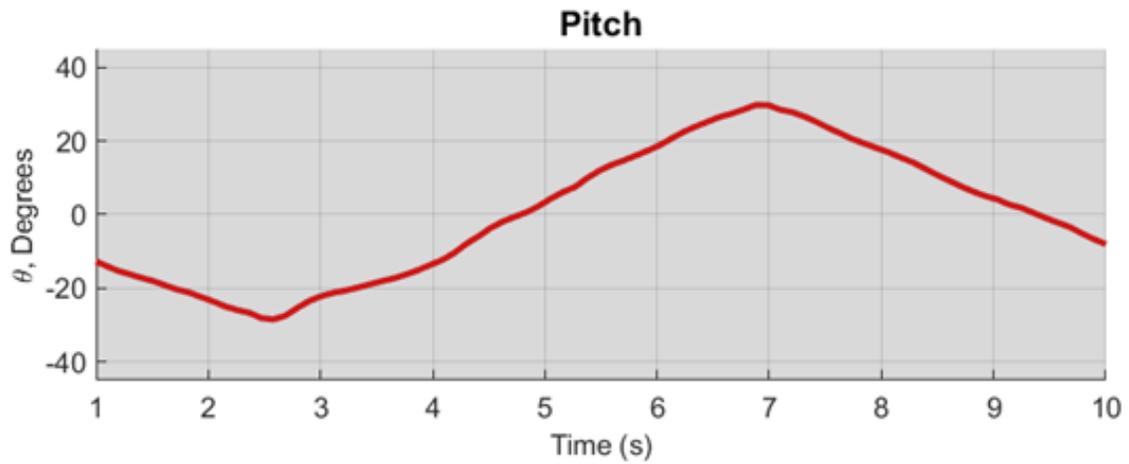


Figure 7: Pitch from -30 degrees to 30 degrees, 2 seconds

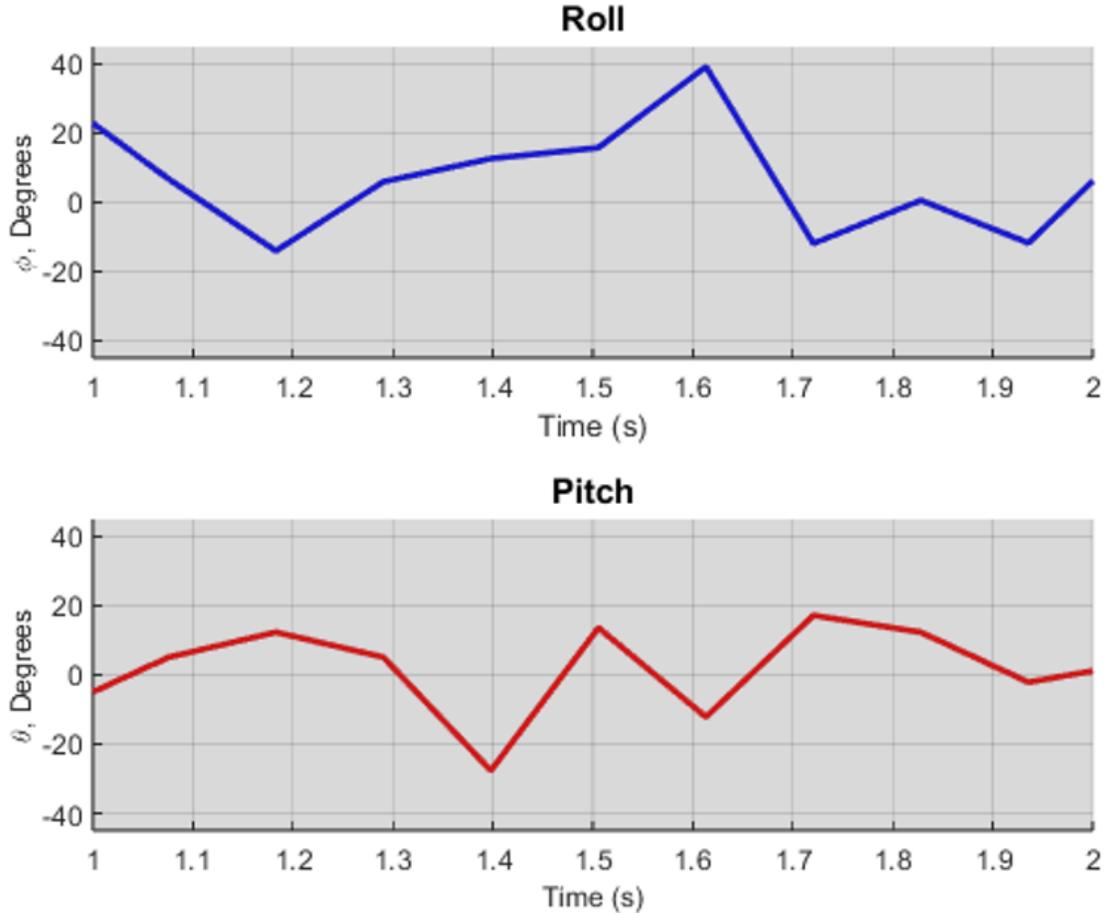


Figure 8: Pitch and Roll from -30 degrees to 30 degrees, 2 seconds

From Figure 6 it is seen that for high frequency oscillation, the filter was not as responsive, producing much more angular lines when roll response was plotted against time. The corresponding low frequency maneuver from Figure 3 was much smoother with rounder peaks. Similarly, from Figure 7 it is seen that pitch estimation also produced angular plots. Combined maneuvering produced similar results.

Conclusion

Implementation of an Extended Kalman Filter (EKF) utilizing an inexpensive IMU and Arduino-based microcontroller is an effective state estimator for certain frequency maneuvers. Through the filtering of sensor noise and accurate estimation of pitch and roll angles, the EKF provides a practical solution for enhancing overall flight stability.

Experimental results showed that the EKF effectively handled low-frequency maneuvers, maintaining smooth and accurate responses for both pitch and roll tests. However, in cases where high frequency of oscillation maneuvers is required around the pitch and roll, the EKF and IMU were slow to respond. This suggests that the current IMU's sampling rate may constrain its performance in highly dynamic scenarios. To better the performance under these

conditions, a more robust IMU utilizing a higher sampling rate would be required. Future improvements to the project could involve expanding the scope to include yaw estimation and finding better tuning parameters of the EKF to further refine the system's robustness and accuracy.

In conclusion, this project highlights the viability of using a low-cost Arduino and IMU in combination with a filtering system to efficiently and accurately estimate future states. It also presents the challenges of using such a system which include limited capabilities and output delay when performing high-frequency maneuvers. Ultimately, this kind of project paves the way for broader accessibility and applicability of drone technology in various industries.

Appendix: MATLAB Code

Listing 1: kalmanfilterintegration.m

```
1 % Plug in arduino first, be sure matlab recognizes it
2 % evaluate each line at a time
3 % Part 1
4 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
5 clear; clc; close all;
6
7 a = arduino; % Connect Arduino to Matlab
8 imu = bno055(a); % Interface BNO-055 IMU with Arduino
9 status = readCalibrationStatus(imu) ; % Calibrate IMU
10 tconversion = 53.76839/500;
11
12 %%%%% Desired Duration %%%%%%%%%%%%%
13
14 % for 10s duration, uncomment these
15 % imu_lim = 94;
16 % tlim = 10;
17
18 % for 30s duration uncomment these
19 imu_lim = 280;
20 tlim = 30;
21
22 % for const streaming, no time limit
23 % imu_lim = 1000000;
24 % tlim = 1000000;
25
26
27 % system declarations / initialization
28
29 h = 0.01; % sample rate
30 Q = 0.001*eye(4); % sensor noise estimation
31 x = getquaternions(0,0) ; % Initialization of quaternions
32 P = 0*eye(4) ; % Initial P val
33 R = 0.001*eye(4) ; % Covariance of measurment sensor
34 pitch = []; %
35 roll = [];
36 H = eye(4);
37
38 % Live plot
39 figure()
40 tiledlayout(2,1);
41 nexttile;
42
43 % Accelerometer (x,y,z)
44 acc_x_line = animatedline;
45 axis([1 tlim -3 3]);
46
47 acc_x_line.LineStyle = '-';
48 acc_x_line.LineWidth = 2;
49 acc_x_line.Color = '[0.99 0.01 0.01]';
```

```

50 acc_x_line_title = title('Accelerometer', 'FontSize', 11);
51 acc_x_line_xlabel = xlabel('Time (s)');
52 acc_x_line_xlabel.FontSize = 9;
53 acc_x_line_ylabel = ylabel('Acceleration (g)');
54 acc_x_line_ylabel.FontSize = 9;
55 set(gca, 'Color', '[0.45 0.45 0.5]');
56 grid on; hold on;
57
58 acc_y_line = animatedline;
59 axis([1 tlim -3 3]);
60
61 acc_y_line.LineStyle = '-';
62 acc_y_line.LineWidth = 2;
63 acc_y_line.Color = '[0.99 0.35 0.01]';
64 acc_y_line_title = title('Accelerometer', 'FontSize', 11);
65 acc_y_line_xlabel = xlabel('Time (s)');
66 acc_y_line_xlabel.FontSize = 9;
67 acc_y_line_ylabel = ylabel('Acceleration (g)');
68 acc_y_line_ylabel.FontSize = 9;
69 set(gca, 'Color', '[0.45 0.45 0.5]');
70 grid on; hold on;
71
72 acc_z_line = animatedline;
73 axis([1 tlim -3 3]);
74
75 acc_z_line.LineStyle = '-';
76 acc_z_line.LineWidth = 2;
77 acc_z_line.Color = '[0.99 0.70 0.01]';
78 acc_z_line_title = title('Accelerometer', 'FontSize', 11);
79 acc_z_line_xlabel = xlabel('Time (s)');
80 acc_z_line_xlabel.FontSize = 9;
81 acc_z_line_ylabel = ylabel('Acceleration (g)');
82 acc_z_line_ylabel.FontSize = 9;
83 set(gca, 'Color', '[0.45 0.45 0.5]');
84 grid on; hold on;
85
86 acc_legend = legend([acc_x_line acc_y_line acc_z_line], {'x axis', 'y axis',
87     , 'z axis'});
88 acc_legend.FontSize = 12;
89 acc_legend.Location = 'northeastoutside';
90 acc_legend.NumColumns = 1;
91 acc_legend.TextColor = 'w';
92 acc_legend.Title.String = 'Accelerometer Data';
93 acc_legend.Title.Color = 'w';
94 acc_legend.Title.FontSize = 11;
95 hold off;
96
97 nexttile;
98 %Gyroscope (x,y,z)
99
100 gyro_x_line = animatedline;
101 axis([1 tlim -10 10]);
102

```

```

103 gyro_x_line.LineStyle = '-';
104 gyro_x_line.LineWidth = 2;
105 gyro_x_line.Color = '[0.01 0.01 0.99]';
106 gyro_x_line_title = title('Gyroscope', 'FontSize', 11);
107 gyro_x_line_xlabel = xlabel('Time (s)');
108 gyro_x_line_xlabel.FontSize = 9;
109 gyro_x_line_ylabel = ylabel('Angular Velocity Rad/s');
110 gyro_x_line_ylabel.FontSize = 9;
111 set(gca, 'Color', '[0.45 0.45 0.5]');
112 grid on; hold on;
113
114 gyro_y_line = animatedline;
115 axis([1 tlim -10 10]);
116
117 gyro_y_line.LineStyle = '-';
118 gyro_y_line.LineWidth = 2;
119 gyro_y_line.Color = '[0.01 0.31 0.99]';
120 gyro_y_line_title = title('Gyroscope', 'FontSize', 11);
121 gyro_y_line_xlabel = xlabel('Time (s)');
122 gyro_y_line_xlabel.FontSize = 9;
123 gyro_y_line_ylabel = ylabel('Angular Velocity Rad/s');
124 gyro_y_line_ylabel.FontSize = 9;
125 set(gca, 'Color', '[0.45 0.45 0.5]');
126 grid on; hold on;
127
128 gyro_z_line = animatedline;
129 axis([1 tlim -10 10]);
130
131 gyro_z_line.LineStyle = '-';
132 gyro_z_line.LineWidth = 2;
133 gyro_z_line.Color = '[0.01 0.70 0.99]';
134 gyro_z_line_title = title('Gyroscope', 'FontSize', 11);
135 gyro_z_line_xlabel = xlabel('Time (s)');
136 gyro_z_line_xlabel.FontSize = 9;
137 gyro_z_line_ylabel = ylabel('Angular Velocity Rad/s');
138 gyro_z_line_ylabel.FontSize = 9;
139 set(gca, 'Color', '[0.45 0.45 0.5]');
140 grid on; hold on;
141
142 gyro_legend = legend([gyro_x_line gyro_y_line gyro_z_line],{'x axis', 'y
    axis', 'z axis'});
143 gyro_legend.FontSize = 12;
144 gyro_legend.Location = 'northeastoutside';
145 gyro_legend.NumColumns = 1;
146 gyro_legend.TextColor = 'w';
147 gyro_legend.Title.String = 'Gyroscope Data';
148 gyro_legend.Title.Color = 'w';
149 gyro_legend.Title.FontSize = 11;
150 hold off;
151
152 % Roll and Pitch Plot %%%%%%%%%%%%%%%
153
154 % Live plot
155 figure()

```

```

156 tiledlayout(2,1);
157 nexttile;
158
159 % Roll
160 roll_line = animatedline;
161 axis([1 tlim -180 180]);
162
163 roll_line.LineStyle = '-';
164 roll_line.LineWidth = 2;
165 roll_line.Color = '[0.1 0.1 0.80]';
166 roll_line_title = title('Roll', 'FontSize', 11);
167 roll_xlabel = xlabel('Time (s)');
168 roll_line_xlabel.FontSize = 9;
169 roll_line_ylabel = ylabel('\phi, Degrees', 'FontSize', 8);
170 roll_line_ylabel.FontSize = 9;
171 set(gca, 'Color', '[0.85 0.85 0.85]');
172 grid on; hold on;
173
174 nexttile;
175
176 % Pitch
177 pitch_line = animatedline;
178 axis([1 tlim -180 180]);
179
180 pitch_line.LineStyle = '-';
181 pitch_line.LineWidth = 2;
182 pitch_line.Color = '[0.80 0.1 0.1]';
183 pitch_line_title = title('Pitch', 'FontSize', 11);
184 pitch_xlabel = xlabel('Time (s)');
185 pitch_xlabel.FontSize = 9;
186 pitch_ylabel = ylabel('\theta, Degrees', 'FontSize', 8);
187 pitch_ylabel.FontSize = 9;
188 set(gca, 'Color', '[0.85 0.85 0.85]');
189 grid on; hold on;
190
191 %Live streaming data
192
193 imu_count = 0;
194 imu_data = [];
195
196 while imu_count < imu_lim
197     imu_count = imu_count + 1;
198
199     imu_read = read(imu); % read imu data
200     imu_matrix = imu_read{:,:};
201     imu_mean=mean(imu_matrix);
202
203     % accelerometer
204     acc_x = imu_mean(:,1);
205     acc_y = imu_mean(:,2);
206     acc_z = imu_mean(:,3);
207
208     acc_x_g = acc_x/9.81;
209     acc_y_g = acc_y/9.81;

```

```

210     acc_z_g = acc_z/9.81 - 1;
211
212     % gyroscope
213     gyro_x = imu_mean(:,4);
214     gyro_y = imu_mean(:,5);
215     gyro_z = imu_mean(:,6);
216
217     gyro_x_deg = rad2deg(gyro_x);
218     gyro_y_deg = rad2deg(gyro_y);
219     gyro_z_deg = rad2deg(gyro_z);
220
221
222     %%%%%%%%%%%          Kalman Filter          %%%%%%%%%%%
223
224     qdot = getqdot(gyro_x,gyro_y,gyro_z,x);
225     xkminus = statePredict(gyro_x,gyro_y,gyro_z,x,h);
226     pminus = pPredict(P,Q,gyro_x,gyro_y,gyro_z);
227     kgain = pminus*inv(pminus+R);
228     z = measureAccel(acc_x,acc_y,acc_z);
229     x = xkminus + kgain*(z-xkminus);
230     [roll(imu_count),pitch(imu_count)] = getEuler(x,imu_count);
231     P = (eye(4) - kgain)*pminus;
232     %%%%%%%%%%%
233
234     % magnetometer
235     mag_x = imu_mean(:,7);
236     mag_y = imu_mean(:,8);
237     mag_z = imu_mean(:,9);
238
239     % orientation
240     ort_x_rad = imu_mean(:,12);
241     ort_y_rad = imu_mean(:,11);
242     ort_z_rad = imu_mean(:,10);
243
244     ort_x = rad2deg(ort_x_rad);
245     ort_y = rad2deg(ort_y_rad);
246     ort_z = rad2deg(ort_z_rad);
247
248     imu_data = [imu_data; [imu_count,acc_x_g,acc_y_g,acc_z_g,...
249         gyro_x, gyro_y,gyro_z,mag_x,mag_y,mag_z,ort_x,ort_y,ort_z]];
250
251     show_imu = [acc_x_g,acc_y_g,acc_z_g,gyro_x, gyro_y,gyro_z,...
252         mag_x,mag_y,mag_z,ort_x,ort_y,ort_z];
253     %disp(show_imu);
254
255     if imu_count == 500
256         disp('END SESSION')
257     end
258
259     addpoints(acc_x_line,imu_count*tconversion,acc_x_g);
260     addpoints(acc_y_line,imu_count*tconversion,acc_y_g);
261     addpoints(acc_z_line,imu_count*tconversion,acc_z_g);
262
263     addpoints(gyro_x_line,imu_count*tconversion,gyro_x);

```

```

264     addpoints(gyro_y_line, imu_count*tconversion, gyro_y);
265     addpoints(gyro_z_line, imu_count*tconversion, gyro_z);
266
267     addpoints(roll_line, imu_count*tconversion, roll(end));
268     addpoints(pitch_line, imu_count*tconversion, pitch(end));
269
270
271     drawnow;
272
273 end
274
275 imu_table = array2table(imu_data, 'VariableNames', {'Time', ...
276     'Acc x', 'Acc y', 'Acc z', 'Gyro X', 'Gyro Y', 'Gyro Z', ...
277     'Mag X', 'Mag Y', 'Mag Z', 'ORT X', 'ORT Y', 'ORT Z'});
278
279
280 %%%%%%%%%%%%%%% Function Calls %%%%%%%%%%%%%%%
281
282 function qq = getquaternions(phi, theta) % create quarternion vector
    given theta and phi
283     qq(1) = sin(phi/2)*cos(theta/2);
284     qq(2) = cos(phi/2)*sin(theta/2);
285     qq(3) = -sin(phi/2)*sin(theta/2);
286     qq(4) = cos(phi/2)*cos(theta/2);
287
288     qq =qq';
289
290 end
291
292 function newQ = statePredict(p,q,r,x,h) % Implement state predictor
    equation of EKF
293     A = (h/2)*[ 2/h,r,-q,p;
294                -r,2/h,p,q;
295                q,-p,2/h,r;
296                -p,-q,-r,h/2] ;
297     newQ = A * x;
298
299 end
300
301 function z = measureAccel(x,y,z) % Determination of Euler angles theta and
    phi from measurment
302     theta = asin(x/9.81);
303     phi = atan2(y,z);
304     z = getquaternions(phi,theta);
305 end
306
307 function p = pPredict(P,Q,p,q,r) % Predict covariance in EKF
308     A = getJacobian(p,q,r);
309
310     p = A*P*A' + Q;
311
312 end
313
314 function A = getJacobian(p,q,r) % Calculation of Jacobian Matrix for EKF

```

```

315     A = 0.5*[ 0,r,-q,p;
316             -r,0,p,q;
317             q,-p,0,r;
318             -p,-q,-r,0] ;
319 end
320
321 function [phi,theta] = getEuler(Q,imu_count) % Calculation of Euler
Angles from updated Quartenrion
322     clc;
323
324     q1 = Q(1);
325     q2 = Q(2);
326     q3 = Q(3);
327     q4 = Q(4);
328
329     a11 = q1^2 - q2^2 - q3^2 + q4^2;
330     a12 = 2 * ( q1 * q2 + q3 * q4 );
331     a13 = 2 * ( q1 * q3 - q2 * q4 );
332     a23 = 2 * ( q2 * q3 + q1 * q4 );
333     a33 = q3^2 - q1^2 - q2^2 + q4^2;
334
335     phi = atan2( a23, a33 );
336     phi = rad2deg(phi);
337     theta = atan2( -a13, sqrt( a11 * a11 + a12 * a12 ) );
338     theta = rad2deg(theta);
339
340     tsec = imu_count *53.768392/500; % time conversion
341
342     fprintf('Pitch is %2.2f degrees \n\n',theta);
343     fprintf('Roll is %2.2f degrees \n\n', phi);
344     fprintf('Current Time Duration: %2.2f s\n\n', tsec);
345 end

```